## MATH 223 Fall 2022 Assignment 29 Due: Friday, December 2

## Reading

Read carefully Section 8.1 "Divergence and Curl" in our text *Multivariable Calculus: A Linear Algebra Based Approach*.

## Writing

Write out careful and complete solutions of Exercises 23 and 30 of Chapter 7 along with Exercises A - D below.

- A. A curve  $\gamma$  has the parametrization  $g(t) = (t, 4 \cos t, 4 \sin t)$ . Sketch the curve, find its curvature and show it is constant.
- **B.** Sketch the curve with parametrization  $g(t) = (t^2, t), -2 \le t \le 2$  and find its curvature. At t = 0 and at  $t = \sqrt{6}$ .
- **C.** Suppose the curve *C* in the plane is the graph of the real-valued function y = f(x) of one variable. Show that its curvature is  $\frac{|f''(x)|}{(1+|f'(x)|^2)^{3/2}}$ .
- **D.** If *C* is a curve in 3-dimensional space with parametrization g(t), show that its curvature is given by  $\frac{|g'(t) \times g''(t)|}{|g'(t)|^3}$ .



PAUL

"He's not seeing anyone right now, due to the curvature of the earth."